سكسّم رياخ (عيد الحب) ١٥/٥/١٥ (كي أستففر الله العظام) م/متار * Find modulus & argument of.

$$\overline{U} = \frac{Z+i}{3+4i}$$

$$|Z| = \frac{|Z|}{|3+4i|} = \frac{|Z|}{|3+4i|} = \frac{\sqrt{2}+i}{\sqrt{3}^2+4^2} = \frac{1}{\sqrt{5}}$$

$$arg(z)$$
 s $arg\left(\frac{2+i}{3+4i}\right) = arg(2+i) - arg(3+4i)$
= $tan^{i}\left(\frac{1}{2}\right) - tan^{-i}\left(\frac{4}{3}\right)$ s - 26.565

$$|Z| = \frac{|1+2i|}{|3-4i|} + \frac{|2-i|}{|5i|} = \frac{|1+2i|}{|3-4i|} + \frac{|2-i|}{|5i|}$$

$$=\frac{\sqrt{1+4}}{\sqrt{25}} + \frac{5}{\sqrt{25}} = \frac{5}{5 \times 5} = \frac{20}{5}$$
 $=\frac{\sqrt{1+4}}{\sqrt{25}} + \frac{5}{\sqrt{25}} = \frac{5}{5 \times 5} = \frac{20}{5}$

sheet I Find & real & imaginary Part & find Polarform $Z = X + iy = Y \left\{ Cos(\theta) + isin(\theta) \right\}$ @z=(1+V3i)6 V= |= |5 |(1+16i)6| = |1+10 \(\overline{3} \) i | 6 = (\overline{1+3})6 = \(\overline{4} \) $\theta = ar2 (1+\sqrt{3}i)^6 = 6 ar2 (1+\sqrt{3}i) = 6 tan^{-1} (\sqrt{3}) = 2\pi$ Z = 64 [Cos (211) + i sin (211)] real -> 69 = 464+0i imaginary -> 0 ففس حل المثال الما مم (1+i) 9

Y= |Z| =

2 show that

a)
$$1+\cos\theta+\cos\theta+\cos\theta+\cos\theta$$
 $e^{i\theta}=\cos\theta+i\sin\theta$

Re $fe^{i\theta}=\cos\theta$

L. H. $s=1+\cos\theta+\cos\theta+\cos\theta+\cos\theta$
 $= Re\left[1+e^{i\theta}+e^{i2\theta}+\cdots+e^{in\theta}\right]$
 $= \sin\theta$
 $= \cos\theta$
 $=$

$$= -\sin\left(\frac{\Theta}{z}\right) - \sin\left(n+i\right)\frac{\Phi}{z}$$

$$-2\sin\frac{\Theta}{z}$$

$$=\frac{1}{2}+\frac{\sin\left(n+\frac{1}{2}\right)\Theta}{2\sin\left(\frac{\Theta}{2}\right)}$$

$$\frac{L.H.5}{e^{\frac{140}{2}}} = \frac{\left(\frac{i30}{e^{\frac{130}{2}}}\right)^{-5}}{\left(\frac{i40}{e^{\frac{12}{2}}}\right)^{12}} = \frac{\left(\frac{i30}{e^{\frac{130}{2}}}\right)^{-5}}{\left(\frac{i40}{e^{\frac{130}{2}}}\right)^{12}} = \frac{\left(\frac{i30}{e^{\frac{130}{2}}}\right)^{-5}}{\left(\frac{i40}{e^{\frac{130}{2}}}\right)^{12}} = \frac{\left(\frac{i30}{e^{\frac{130}{2}}}\right)^{-5}}{\left(\frac{i30}{e^{\frac{130}{2}}}\right)^{-5}} = \frac{\left(\frac{i30}{e^{\frac{130}{2}}}\right)^{-5}}{\left(\frac{i30}{e^{\frac$$

[4] show that [Z,+Zz]2+ |Z,-Zz|2=2 |Z,|2+2 |Zz|2 L.H.S = |Z,+Z2|2+|Z,-Z2|2 $=(Z_1+Z_2)(Z_1+Z_1)+(Z_1-Z_2)(Z_1-Z_1)$ $=(Z_1+Z_2)(\bar{Z}_1+\bar{Z}_2)+(Z_1-Z_2)(\bar{Z}_1-\bar{Z}_2)$ = Z, Z, + Z, Z, + Z, Z, + Z, Z, + Z, Z, - Z, Z, - Z, Z,

L.H.S = $|Z_1|^2 + |Z_2|^2 + |Z_1|^2 + |Z_2|^2$ = $2|Z_1|^2 + 2|Z_2|^2$

De Moiver theorem to obtain Cosso & sing in terms of power of Cas &. > (cose tisine) = cos nettisimo) (cose + i sine) = cos 30 + i sin(30) (a+b)3 = Ma 2 +32 b +3ab2 +b3 a=Cos O bisin 0 = Cos0 + Cos0 *sin0 + - 3 cos sin0 + - i sin0 = Cos 30 + i sin(30) Cosso = Cos 0 - 3 Cos sino = Cos = - 3 Cos & [1- Cos 0 -1(CASA) ~4

 $3\cos\theta \sin\theta - \sin^3\theta = \sin^3\theta$ $\frac{\sin^3\theta}{\sin\theta} = 3\cos^2\theta - \sin^2\theta$ $= 3\cos^2\theta - (1-\cos^2\theta)$ $= 4\cos^2\theta - 1$